

1. Basic Geometrical Properties

◆ Sum of angles at a point = 360°

Explanation: The angles around a single point form a full circle.

Example: If three angles around a point are 120° , 110° , and 90° , find the unknown angle.

- $\text{Sum} = 120^\circ + 110^\circ + 90^\circ = 320^\circ$
 - $\text{Unknown angle} = 360^\circ - 320^\circ = 40^\circ$
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◆ Sum of angles on a straight line = 180°

Explanation: Adjacent angles on a straight line are supplementary.

Example: If one angle is 130° , the other angle on the straight line is:

- $180^\circ - 130^\circ = 50^\circ$

◆ Vertically opposite angles are equal

Explanation: When two straight lines intersect, the opposite angles are equal.

Example: If angle A = 70° , then the vertically opposite angle is also:

- 70°

◆ Angle sum of a triangle = 180°

Explanation: The interior angles in every triangle always add up to 180° .

Example: If two angles are 65° and 45° , the third angle is:

- $180^\circ - (65^\circ + 45^\circ) = 180^\circ - 110^\circ = 70^\circ$

□ 2. Angles in Parallel Lines

Let's consider two parallel lines cut by a transversal.

◆ Corresponding angles are equal

Explanation: They are in matching corners ("F" shape).

Example: If one corresponding angle is 110° , the angle in the matching corner is also:

- 110°

◆ Alternate angles are equal

Explanation: They are on opposite sides of the transversal ("Z" shape).

Example: If one alternate angle is 75° , then the angle on the other side is also:

- 75°

◆ Co-interior (same-side interior) angles sum to 180°

Explanation: These angles lie on the same side of the transversal inside the parallel lines ("C" shape).

Example: If one co-interior angle is 115° , the other is:

- $180^\circ - 115^\circ = 65^\circ$

◆ Angle sum of a quadrilateral = 360°

Explanation: The sum of the interior angles of any four-sided shape is 360° .

Example: If three angles are 100° , 85° , and 95° , the fourth angle is:

- $360^\circ - (100^\circ + 85^\circ + 95^\circ) = 360^\circ - 280^\circ = 80^\circ$

◡ 3. Angle Properties of Polygons

◆ Interior angle of a regular polygon:

$$\text{Interior angle} = \frac{(n - 2) \times 180^\circ}{n}$$

Where n = number of sides.

Example: A regular hexagon (6 sides):

$$\text{Interior angle} = \frac{(6 - 2) \times 180}{6} = \frac{720}{6} = **120^\circ**$$

◆ Exterior angle of a regular polygon:

$$\text{Exterior angle} = \frac{360^\circ}{n}$$

Example: A regular octagon (8 sides):

$$\text{Exterior angle} = \frac{360}{8} = **45^\circ**$$

◆ Sum of interior angles of any polygon:

$$\text{Sum} = (n - 2) \times 180^\circ$$

Example: A 7-sided polygon:

$$\text{Sum} = (7 - 2) \times 180 = **900^\circ**$$

◆ 3-Letter Notation:

Use it to describe angles clearly, e.g., $\angle ABC$ means the angle at point B, between line segments AB and BC.